

# The Misallocation of Pay and Productivity in the Public Sector: Evidence From the Labor Market for Teachers

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# Motivation

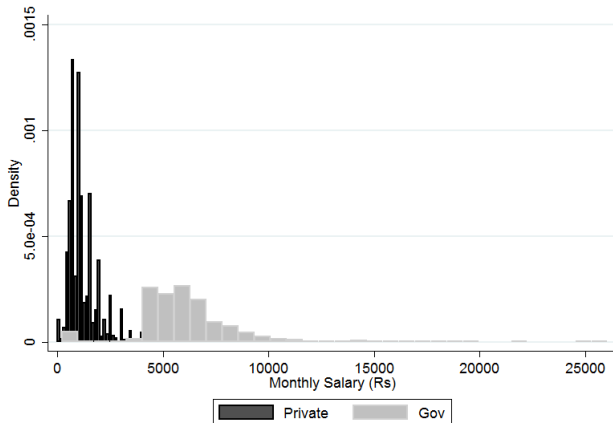
- Important and contentious policy question: how to recruit and retain high quality teachers.
  - Typical solution: higher salaries.
  - But others argue that that public school teachers are overpaid (Biggs and Richwine, 2011).
- Particularly important for low-income countries: teacher salaries account for 80 percent of educational expenditures.
- In light of this debate, we need to know:
  - What teacher characteristics are associated with teacher effectiveness and whether teachers are rewarded for them.
  - Would average teacher quality fall if baseline salaries declined?

# LEAPS Data

Two key surveys in 112 villages of Punjab Province, Pakistan, each conducted every year from 2003-2007:

- Geo-coded survey of the universe of schools.
  - 574 sex-segregated public schools and 1,533 public school teachers in 112 villages.
  - Data on school and teacher characteristics.
- Surveys of children in the schools, including low-stakes test scores in math, Urdu, and English.
  - 22,857 children in public schools.

# Teacher Salaries in 2004



# TVA Estimation

Estimate:

$$y_{ijt} = \beta_0 + \sum_a \beta_a y_{ij,t-1} I(\text{grade} = a) + \gamma_j + \alpha_t + \mu_g + \epsilon_{ijt}.$$

- $i$  denotes a student,  $j$  denotes a teacher, and  $t$  denotes a school.
- $y_{ijt}$  is student  $i$ 's test score in year  $t$ .
- $\gamma_j$  is the teacher fixed effect or the teacher value-added.
- $\alpha_t$  is the round fixed effect.
- $\mu_g$  is the grade fixed effect.

Key assumption:  $\epsilon_{i,t} \perp \gamma_j$ .

# TVA Robustness

- **Omitted variable bias test # 1:** Including controls for class-size, peer quality, and socioeconomic characteristics has little effect on the estimates.
- **Omitted variable bias test # 2:** The TVA of school-changers' future teachers does not predict current TVA.
- **Specification test:** TVAs are highly predictive of school-changers' test score gains.

# How Important is Teacher Quality?

- The variance of the TVAs also tells us about the importance of teacher quality in low income countries.
- With a sampling error correction, a 1 SD better teacher will increase mean student test scores by 0.16 sd.

▶ Sampling Error Calculation

- Higher end of still substantial variance in teacher quality in the U.S. (Rothstein, 2004; Chetty et al., 2014).

# Association Between Teacher Characteristics and TVA

	(1) Mean TVA	(2) Mean TVA	(3) Mean TVA	(4) Mean TVA	(5) Mean TVA
<i>Female</i>	0.070*** (0.026)	-0.036 (0.134)	0.080*** (0.026)	0.207 (0.225)	
<i>Local</i>	0.025 (0.025)	0.008 (0.031)	0.024 (0.028)	-0.004 (0.049)	
<i>Some Teacher Training</i>	-0.023 (0.055)	-0.101 (0.072)	-0.093 (0.075)	-0.213* (0.126)	
<i>Has BA or Better</i>	0.054** (0.025)	0.043 (0.031)	0.012 (0.033)	0.010 (0.059)	
<i>Had &gt; 3 Years of Exp in 2007</i>	0.060 (0.038)	0.076 (0.052)	0.037 (0.047)	0.163* (0.097)	
<i>Temporary Contract</i>	-0.003 (0.036)	0.049 (0.048)	-0.020 (0.043)	0.051 (0.083)	
<i>Mean English Test Score</i>			0.032** (0.015)	0.015 (0.022)	
<i>Mean Urdu Test Score</i>			0.034 (0.023)	0.013 (0.037)	
<i>Mean Math Test Score</i>			0.023 (0.022)	-0.013 (0.034)	
<i>Have 0 or 1 Years Exp.</i>					-0.305** (0.135)
<i>Lagged Mean Score</i>					0.717*** (0.013)
Fixed Effects	District	School	District	School	Teacher
Number of Observations	1,383	1,383	919	919	27,089
Adjusted R Squared	0.224	0.450	0.228	0.415	0.721
Clusters	471	471	469	469	583
F	2.031	1.194	2.533	0.602	



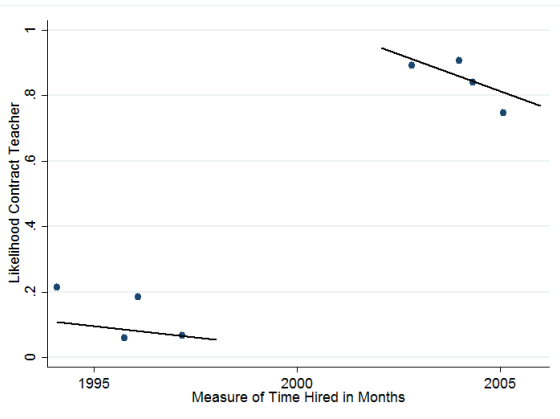
# Effect of TVA on Teacher Salaries

	(1) Log Salary Public	(2) Log Salary Public	(3) Log Salary Public	(4) Log Salary Public	(5) Log Salary Private
<i>Mean TVA</i>		-0.007 (0.014)	-0.028 (0.025)	-0.044 (0.036)	0.111** (0.046)
<i>Female</i>	-0.036*** (0.013)	-0.035*** (0.013)	0.154** (0.070)	0.054 (0.094)	-0.413*** (0.043)
<i>Local</i>	-0.052*** (0.019)	-0.051*** (0.019)	-0.049 (0.032)	-0.019 (0.043)	-0.178*** (0.029)
<i>Some Teacher Training</i>	0.518*** (0.141)	0.518*** (0.141)	0.392*** (0.140)	0.837*** (0.316)	0.165*** (0.045)
<i>Has BA or Better</i>	0.255*** (0.019)	0.255*** (0.019)	0.263*** (0.028)	0.211*** (0.042)	0.334*** (0.045)
<i>Had &gt; 3 Years of Exp in 2007</i>	0.063 (0.042)	0.064 (0.042)	0.120* (0.064)	0.122 (0.101)	0.020 (0.029)
<i>Temporary Contract</i>	-0.354*** (0.032)	-0.355*** (0.032)	-0.327*** (0.059)	-0.308*** (0.092)	
<i>Age</i>	0.058*** (0.015)	0.058*** (0.015)	0.063*** (0.020)	0.039 (0.029)	0.016** (0.007)
<i>Age<sup>2</sup></i>	-0.000*** (0.000)	-0.000*** (0.000)	-0.001** (0.000)	-0.000 (0.000)	-0.000** (0.000)
<i>Mean English Score</i>				0.016 (0.017)	
<i>Mean Urdu Score</i>				-0.006 (0.029)	
<i>Mean Math Score</i>				0.020 (0.025)	
Fixed Effects	District	District	School	School	District
Adjusted R Squared	0.616	0.615	0.662	0.707	0.459
Number of observations	1,383	1,383	1,383	919	807
F	108.304	96.471	35.025	12.496	38.522
Clusters	471	471	471	469	294

# How Elastic is the Teacher Labor Supply?

- Our TVA results suggest that there is little link between teacher salaries and teacher quality.
- Raises an important policy question: How would lowering teacher salaries affect the quality of teachers?
- A regime change following Pakistan's unexpected nuclear tests in 1998 allows us to look at the joint effect of a salary decrease combined with greater accountability.

# Effect of the Regime Change on Teacher Contracts



# Estimation Strategy

- First stage:

$$\begin{aligned} \textit{TemporaryContract}_j = & \delta_0 + \delta_1 \textit{Post}_j + \delta_2 \textit{month\_hired}_j + \\ & \delta_3 \textit{month\_hired}_j \times \textit{Post}_j + \alpha_d + \mu_j, \end{aligned}$$

where  $\textit{Post}_j$  is an indicator variable equal to 1 if a teacher is hired after 1998 and 0 otherwise and  $\alpha_d$  is a district fixed effect.

- Second stage:

$$\begin{aligned} \textit{TVA}_j = & \beta_0 + \beta_1 \textit{TemporaryContract}_j + \beta_2 \textit{month\_hired}_j + \\ & \beta_3 \textit{month\_hired}_j \times \textit{Post}_j + \alpha_d + \epsilon_j. \end{aligned}$$

# Effect on TVA

	(1)	(2)	(3)	(4)	(5)	(6)
	Mean TVA	SE	N	Within School Mean TVA	SE	N
OLS (Full Sample)	-0.004*	0.042	1,337.000	0.024*	0.026	1,278
RD (Full Sample)	-0.004	0.052	1,337.000	0.056	0.041	1,278
RD (2 Year)	0.840	0.550	227.000	0.360	0.322	201
RD (3 Year)	0.219	0.241	376.000	0.254**	0.123	336
RD (4 Year)	0.350	0.234	393.000	0.193*	0.097	350

# Effects of Contract Status on Sorting

- **Individuals to teaching:** No discontinuous change in teacher characteristics.
- **Teachers to schools:** Contract teachers assigned to smaller schools with fewer teachers and less facilities.
- **Students to teachers:** Some evidence that contract teachers' students' have less educated fathers.

# Is the Quality of Contract Teachers Declining Over Time?

Estimate:

$$y_{ijt} = \beta_0 + \beta_1 \text{month\_hired}_j + \beta_2 \text{Post}_j + \beta_3 \text{Post}_j * \text{month\_hired}_j + \sum_g \beta_g y_{i,t-1} I(\text{grade} = g) + \alpha_t + \epsilon_{ijt}.$$

- Sample: teacher-year observations where contract teachers have 0 or 1 years of experience and all permanent teachers.
- Include permanent teachers to identify round fixed effects in case student test scores are increasing over time.
- Coefficient of interest:  $\beta_3$  captures the effect of being hired later after the policy change.

# Is the Quality of Contract Teachers Declining Over Time?

	(1) Mean Test Scores
<i>Month Hired</i>	0.002** (0.001)
<i>Month Hired</i> × $I(\text{Year Hired} > 2001)$	-0.007 (0.024)
$I(\text{Year Hired} > 2001)$	Y
Round FE	Y
District FE	Y
Grade by Lagged Test Score Interactions	Y
Number of Observations	21,788
Adjusted R Squared	0.660
Clusters	450

No evidence that contract teacher quality is decreasing over time.



# Conclusion

- Teacher quality is important in low-income countries.
- As in the United States, besides experience, most observable teacher characteristics do not predict quality.
- Teacher salaries are not related to teacher quality.
- A regime change shows that the teacher supply is highly inelastic at current wages.
- Students of teachers hired on 35 percent lower salaries perform as well or better than students of permanent teachers.

# LEAPS Testing Structure

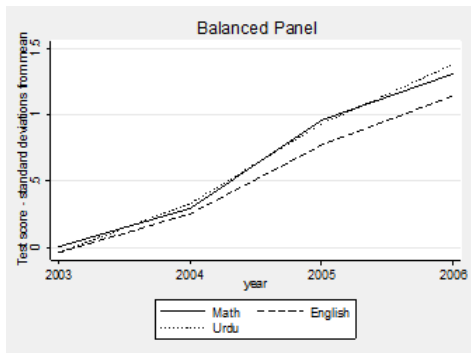
	(1) Number of Teachers	(2) Number of Students	(3) Teachers in Schools With > 1 Teacher With Tested Students	(4) Students in Schools With > 1 Teachers With Tested Students
Round 1	487	8,341	7	171
Round 2	592	9,309	219	3,350
Round 3	1,007	16,904	879	15,249
Round 4	1,085	15,239	875	13,110

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## Public School Students Used in TVA Estimation

Grade	Rounds		
	<u>Student-Years</u>		
	2	3	4
1	1	1	0
2	3	1	5
3	347	34	364
4	6,676	1,135	6,449
5	6	6,373	865
6	0	5	4,653
7	0	0	8

# Learning Over Time

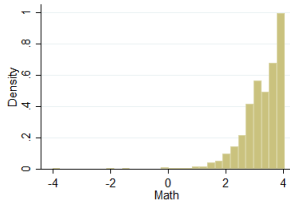
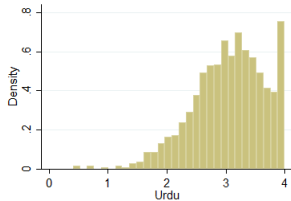
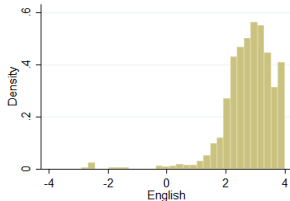


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# What Does a Test Score Mean?

	Year 1 Prop correct	Year 2 Prop correct	Year 3 Prop correct	Year 4 Prop correct
<b>Total kids</b>	6,038	6,038	6,038	6,038
<b>English</b>				
Eng 12: Match picture with word, Banana	0.631	0.75	0.834	0.873
Eng 18: Fill missing letter for picture, Cat	0.68	0.743	0.817	0.853
Eng 19: Fill missing letter for picture, Flag	0.287	0.299	0.478	0.554
Eng 30: Fill missing word in sentence	0.276	0.332	0.441	0.535
Eng 43: Construct sentence with word 'deep'	0.01	0.014	0.037	0.108
Eng 44: Construct sentence with word 'play'	0.024	0.027	0.113	0.218
	0.318	0.361	0.453	0.524
<b>Math</b>				
Math 1: Count number of moons, write number	0.622	0.687	0.797	0.749
Math 9: Add 3 + 4	0.903	0.91	0.951	0.94
Math 12: Multiply 4 x 5	0.603	0.641	0.759	0.811
Math 24: Add 36 + 61	0.855	0.878	0.922	0.93
Math 25: Add 678 + 923	0.561	0.595	0.712	0.745
Math 27: Subtract 98 - 55	0.698	0.756	0.826	0.856
Math 30: Multiply 32 x 4	0.522	0.569	0.703	0.756
Math 32: Divide 384 / 6	0.193	0.245	0.456	0.541
Math 34: Cost of necklace, simple algebra	0.092	0.148	0.257	0.278
Math 39: Convert 7/3 into mixed fractions	0.014	0.046	0.07	0.145
	0.5063	0.5475	0.6453	0.6751
<b>Urdu</b>				
Urdu 3: Match picture with word, Book	0.739	0.822	0.916	0.946
Urdu 4: Match picture with word, Banana	0.736	0.824	0.906	0.945
Urdu 5: Match picture with word, House	0.538	0.601	0.679	0.755
Urdu 10: Combine letters into word	0.737	0.792	0.861	0.897
Urdu 12: Combine letters into word	0.372	0.45	0.537	0.627
Urdu 19: Antonyms, Chouta	0.44	0.502	0.688	0.792
Urdu 20: Antonyms, Khushk	0.368	0.493	0.623	0.693
Urdu 36: Complete passage for grammar	0.293	0.391	0.563	0.678

# Teacher Knowledge



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## Alternative Methods I: Empirical Bayes (Chetty et al., 2004; Kane and Staiger, 2008)

- Multiply noisy estimate of TVA (such as TVA generated by our method) by an estimate of its reliability.
- Estimate reliability as ratio of signal (TVA) variance to signal plus noise (student and year variance).
- Within classroom variance gives student variance.
- Covariance between average residual in teacher's class in  $t$  and  $t - 1$  gives teacher variance.
- Variance of classroom component is the remainder of the residual's variance.

## Alternative Methods I: Empirical Bayes (Chetty et al., 2004; Kane and Staiger, 2008)

### Problems:

- Estimating teacher variance this way requires that a teacher's quality is time-invariant.
- To satisfy this assumption, authors include experience fixed effects.
- We cannot control for experience without subsuming the contract effect.
- Instead, teacher fixed effects capture mean teacher quality over the surveyed period, including mean experience effects.



## Alternative Methods II: Child Fixed Effects (Rockoff, 2004)

- Method:
  - Include child fixed effects in the TVA estimating equation to further control for selection.
- Problem:
  - Relies on children switching teachers.
  - In Pakistan, teachers teach multiple grades, so this reduces the effective sample by 54 percent.
  - Mis-entered teacher ids may dominant the new sample, biasing estimates.

## Alternative Methods II: Child Fixed Effects (Rockoff, 2004)

For example, assume:

- Students are identical and TVA is randomly distributed.
- A student has a probability  $p = 0.1$  of changing teachers each year.
- An ID has a probability  $e = 0.01$  of being incorrectly entered.

Then, there are three cases where a change appears to take place:

- Id was incorrectly entered and no change occurs: probability =  $0.01 \times 0.9 = 0.009$
- Id is correctly entered and a change happens: probability =  $0.99 \times 0.1 = .099$
- Id is incorrectly entered and a change occurred: probability =  $0.1 \times 0.01 = 0.001$

So, the probability a teacher id is mis-attributed in the effective sample is  $\frac{0.01}{(0.009+0.099+0.001)} = 0.09$

## Alternative Methods II: Child Fixed Effects (Rockoff, 2004)

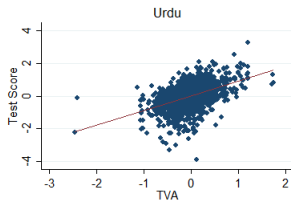
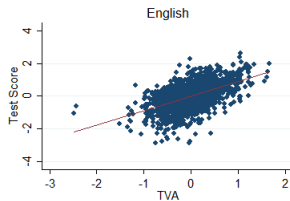
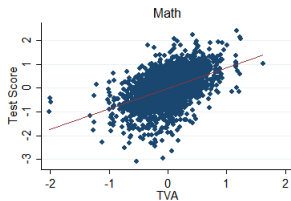
More generally, assume:

- Students are identical and TVA is randomly distributed.
- A student has a probability  $p$  of changing teachers each year.
- An ID has a probability  $e$  of being incorrectly entered.

Then,

$$E(\widehat{TVA}_j) = \frac{p}{e(1-p) + p(1-e) + ep} TVA_j + \frac{e}{e(1-p) + p(1-e) + ep} \overline{TVA}_j.$$

# Graphical Results



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## Sampling Error

$$\phi = E(\hat{\phi}) - \frac{1}{M} \sum_{js} \left( \frac{\sigma^2}{N_{js}} \left( 1 - \frac{1}{T_s} \right) + \frac{1}{T_s^2} \sum_{d=1}^{T_s} \frac{\sigma^2}{N_{ds}} \right).$$

- $\phi$  is the variance of the true TVAs.
- $M$  is the number of teachers.
- $N_{js}$  is the number of students of a teacher  $j$  in a school  $s$ .
- $\sigma^2$  is the variance of idiosyncratic shocks at the student-level.
- $T_s$  is the number of teachers in a school  $s$ .