



### Measuring Destitution in Developing Countries: An Ordinal Approach for Identifying Linked Subset of Multidimensionally Poor

Sabina Alkire, Adriana Conconi and Suman Seth

Inequality – Measurement, Trends, Impacts, and Policies UNU-WIDER, Helsinki, September 2014



### Motivation

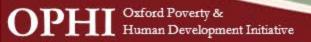
Understanding different degrees and kinds of poverty contributes to their removal

Poorest of the poor are characteristically different and may require different types of assistance

– Lipton (1983), Devereux (2003), Harris-White (2005)

Deprivations among the poorest may reflect more chronic form of deprivations

McKay and Lawson (2003); Aliber (2003)





### Recent Debates and Goals

#### World Bank Aims ending \$1.25/day poverty by 2030 – Jim Yong Kim, President of the World Bank

Shared prosperity/inclusive economic growth

- Tracking income growth among nation's bottom 40 percent

"MDGs <u>did not focus</u> enough on reaching the <u>very</u> <u>poorest</u>"

High-Level Panel on the Post-2015 Development Agenda (2013)



### Certain Concerns Remain

- 1. Does reducing \$1.25/day automatically reduce deprivations in <u>other</u> dimensions? <u>Multidimensionality</u>!
- 2. Is it sufficient to look at deprivations in different dimensions <u>separately</u>? Joint distribution of deprivations!
- 3. What method is appropriate that respects the <u>ordinal</u> nature of the data in practice? Counting Approach!
- 4. Does the overall improvement ensure improvement among the situation of the <u>poorest</u>? Assessing Destitution!



# In This Paper

#### Methodological concern

- How do we legitimately use ordinal information (without 'cardinalizing' ordinal data inappropriately) to identify the destitute
- Our approach is based on the <u>dual cut-off</u> counting approach to identification developed by Alkire and Foster (2011)

#### Distributional concern

- How has poverty reduced among the 'destitute', in comparison with overall poverty
- Has the 'destitute' being left behind?

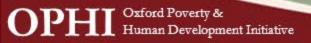


### How are the Poorest of the Poor Referred?

#### Various terms are used

- Ultra poor (Lipton 2003 and others)
- Destitute (Devereux 2003, Harris-White 2005)
- Extreme Poor (World Bank \$1.25 a day)
- No agreement on the *hierarchy* of these terms
- We use the term 'destitute' which has been presented as a more multidimensional concept

Devereux (2003), Harris-White (2005)





# Literature on Identification of Ultra Poor

#### Lipton (1983, 1988)

- Those eating below 80% of <u>dietary energy requirements</u>, and spending 80% or more total income on food
- Similar definitions by Kakwani (1993) and Ellis (2012)

#### **Other Monetary Approaches**

Cornia (1994), Klasen (1997), Roberts (2001) and Aliber (2003),
IFPRI (2007), Harrigan (2008), Bird and Manning (2008), Foster and Smith (2013)

#### Multiple Inclusion Criteria (NGOs)

- BRAC in Bangladesh (Haldar and Mosley 2004, BRAC 2007)

Bandhan in a district of India (Banerjee et al. 2011)



### Literature on Identification of Destitute

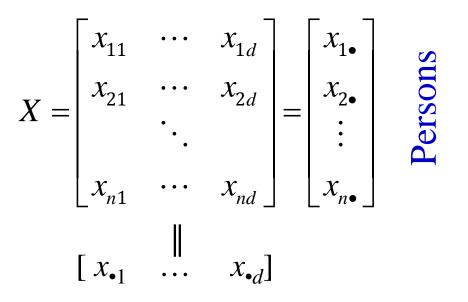
Devereux (2003) proposes identifying destitute using: inability to meet subsistence needs, assetlessness, and dependence on transfers (does not propose any particular method)

Ellis (2012) identify those households who are ultra poor and have labour dependency ratio of four or more as destitute

In this paper, we use the counting approach framework to identify the destitute

UNIVERSITY OF OXFORD

#### Dimensions



#### A general achievement matrix

 $x_{ij}$ : the achievement of individual *i* in dimension *j* 

#### Example:

 $x_{1d}$ : the achievement of the *first* individual in dimension *d* 

 $x_{n1}$ : the achievement of the  $n^{\text{th}}$ individual in the *first* dimension



#### Dimensions

#### **Deprivation cutoffs (First)**

 $X = \begin{bmatrix} x_{11} & \cdots & x_{1d} \\ x_{21} & \cdots & x_{2d} \\ & \ddots & \\ x_{n1} & \cdots & x_{nd} \end{bmatrix} = \begin{bmatrix} x_{1} \\ x_{2} \\ \vdots \\ x_{n} \end{bmatrix}$  Solve  $z_j$ : deprivation cutoff in dimension jif  $x_{ij} < z_j$  $\begin{bmatrix} x_{\bullet 1} & \dots & x_{\bullet d} \end{bmatrix}$  $z = [z_1 \quad \dots \quad z_d]$ 

 $z_i$ : deprivation cutoff in dimension j

if  $x_{ii} < z_i$ 

Deprivation status value:  $g_{ii} = 1$  if deprived and  $g_{ii} = 0$  if not



#### Dimensions

#### **Deprivation cutoffs (First)**

 $g = \begin{bmatrix} g_{11} & \cdots & g_{1d} \\ g_{21} & \cdots & g_{2d} \\ & \ddots & \\ g_{n1} & \cdots & g_{nd} \end{bmatrix} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $g_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{2} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ \vdots \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1} \\ g_{n} \\ g_{n} \end{bmatrix}$   $f_{i} = \begin{bmatrix} g_{1$  $\begin{bmatrix} g_{\bullet 1} & \cdots & g_{\bullet d} \end{bmatrix}$  $z = [z_1 \quad \dots \quad z_d]$ 

 $z_i$ : deprivation cutoff in dimension j

Deprivation status value:  $g_{ii} = 1$  if deprived and  $g_{ii} = 0$  if not



Weights or relative values  $w = (w_1, ..., w_d)$  are assigned

Deprivation score for person *i* is obtained as  $c_i = \sum_j w_j g_{ij}$ – Deprivation score signifies the magnitude of deprivations

Poverty cutoff (Second cutoff): *k* 

- Person *i* is identified as poor if  $c_i \ge k$ , non-poor otherwise

Set of poor denoted by Z



#### Identification of the poor

# Identification function: $\rho(x_i; z, w, k) = 1$ for $i \in Z$ and $\rho(x_i; z, w, k) = 0$ , otherwise

- $\succ$  Deprivation cutoffs: *z*
- > Poverty cutoff: k
- $\succ$  Weights: w

UNIVERSITY OF OXFORD

### How to Identify Destitute (Subset of Poor)?

- Denote the set of destitute by  $\underline{Z} \subseteq Z$
- Identification of destitute:  $\rho(x_i;\underline{z},\underline{w},\underline{k}) = 1$  for  $i \in \underline{Z}$  and  $\rho(x_i;\underline{z},\underline{w},\underline{k}) = 0$ , otherwise

→ Destitute deprivation cutoff: <u>z</u>

> Destitute poverty cutoff:  $\underline{k}$ 

 $\succ$  Weight vector: <u>w</u>

- In order to have  $\underline{Z} \subseteq Z$ , we require that  $\underline{w} = w$ ,  $\underline{z} \le z$ , and  $\underline{k} \ge k$ 
  - Non union criterion



# Identifying a Subset of the Poor

#### The intensity approach

- Identify those who are more intensely poor with the set of same deprivation cutoffs
- ➤ Uses the deprivation cutoff vector z but a more stringent poverty cutoff <u>k</u> ≥ k
- ► Identification function:  $\rho_i(x_i; z, w, \underline{k}) = 1$  for  $i \in \underline{Z}$  and  $\rho_i(x_i; z, w, \underline{k}) = 0$ , otherwise
- Application: Human Development Report (2010)



# Identifying a Subset of the Poor

#### The **depth** approach

- Identify those having multiple deprivations with larger depth of deprivations
- > Uses the deprivation cutoff vector  $\underline{z} \leq z$
- ≻ Obtain deprivation status value:  $\underline{g}_{ij} = 1$  if  $x_{ij} \leq \underline{z}_j$ , else  $\underline{g}_{ij} = 0$
- ► Obtain *deprivation score*:  $\underline{c}_i = \sum_j w_j \underline{g}_{ij}$
- ≻ Identify person *i* as depth poor iff  $\underline{c}_i \ge \underline{k}$  such that  $\underline{k} \ge k$
- ► Identification function:  $\rho_i(x_i;\underline{z},w,\underline{k}) = 1$  for  $i \in \underline{Z}$  and  $\rho_i(x_i;\underline{z},w,\underline{k}) = 0$ , otherwise



# Identifying a Subset of the Poor

#### The **mixed** approach

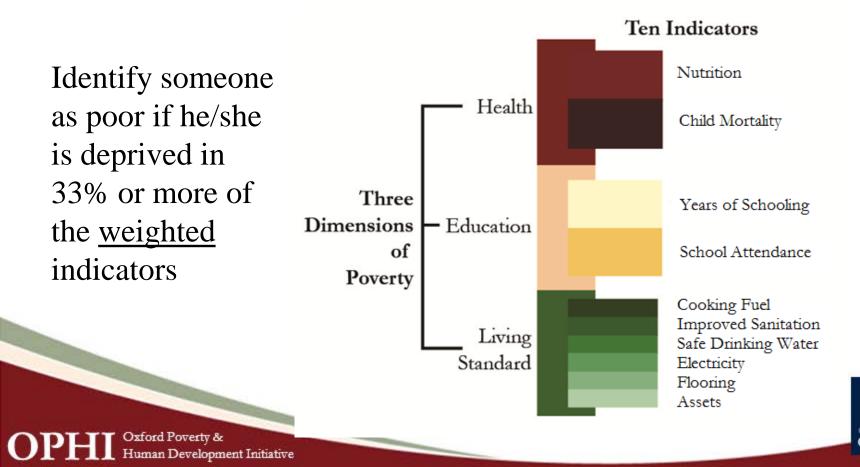
- > Identify the set of intensity poor  $\underline{Z}_I$  with  $(z, w, \underline{k})$
- ≻ Identify the set of depth poor  $\underline{Z}_E$  with  $(\underline{z}, w, \underline{k}')$  and  $\underline{k} \leq \underline{k}' \leq k$
- The subset of poor  $\underline{Z}$  can be identified as the <u>intersection</u> of the intensity poor and depth poor such that  $\underline{Z} = \underline{Z}_I \square \underline{Z}_E$
- > Application: Alkire and Seth (2013)

A more robust way to identify the poorest



### Identification of the Poor in MPI

Develop a deprivation profile for each person, using a set of indicators, cutoffs and weights (Alkire and Santos 2010)

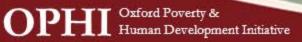


### Deprivation cutoffs: MPI

<b>Deprivation Cutoff</b> (z)	
No household member has completed five years of schooling	
Any school-aged child in the household is not attending school up to class 8	
Any woman or child in the household with nutritional information is	
undernourished	
Any child has passed away in the household	
The household has no electricity	
The household's sanitation facility is not improved or it is shared with other	
households	
The household does not have access to safe drinking water, or safe water is	
more than a 30-minute walk (round trip)	
The household has a dirt, sand, or dung floor	
The household cooks with dung, wood, or charcoal	
The household owns at most one radio, telephone, TV, bike, motorbike, or	
refrigerator; and does not own a car or truck	

UNIVERSITY OF

OXFORD



# Deprivation Cutoffs: Destitute

Indicator	Deprivation Cutoff ( <u>z</u> )	
Schooling	No one completed <b>at least one</b> year of schooling (>=1)	
Attendance	No child attending school up to the age at which they should finish class 6	
Nutrition	Severe Undernourishment of any adult ( <u>BMI&lt;17kg/m<sup>2</sup></u> ) or any child	
	(-3 standard deviations from median)	
Mortality	<u>2 or more</u> children died in the household	
Electricity	The household has no electricity (No change)	
Sanitation	There is no facility/bush, or other (open defecation)	
Water	The household does not have access to safe drinking water, or safe water is	
	more than a <u>45-minute</u> walk (round trip)	
Floor	The household has a dirt, sand, or dung floor (No change)	
Cooking fuel	The household cooks with dung or wood	
	(coal/lignite/charcoal are now non-deprived)	
Assets	The household has <b>no assets (radio, mobile phone, etc.)</b> and no car	



### Destitution

We have implemented a destitution measure using the *depth approach* across 49 countries

> Indicators:	Same as MPI
≻Weights:	Same as MPI
> Poverty cutoff:	Same as MPI
Deprivation cutoffs:	Deeper

All 'destitute' people are already poor



### Data Coverage

49 countries cover 2.8 billion people in the world, including populous countries such as India, Indonesia, Pakistan, Nigeria and Bangladesh

These 49 countries contain 1.2 billion MPI poor



### At-A-Glance

Half of the 1.2 Billion MPI poor people are destitute

Of these destitute, 97.3% live in Sub-Saharan Africa and South Asia; over half of them live in India.

The percentage of MPI poor who are destitute:Sub Saharan Africa: 53.3%South Asia:Latin America and Caribbean: 25.3%East Asia &Europe & Central Asia: 18.7%Arab countrest

South Asia: **50.6%** East Asia & Pacific: **26.4%** Arab countries: **12.3%** 

> UNIVERSITY OF OXFORD

### How Deprived the Destitute Are?

- The proportion of population destitute:  $\underline{H}$
- The proportion of population destitute <u>and</u> deprived in indicator *j* by the depth indicator:  $\underline{h}_i(\underline{k})$
- Then, the proportion of destitute deprived in indicator *j* by the depth indicator:  $\underline{h}_j(\underline{k})/\underline{H}$



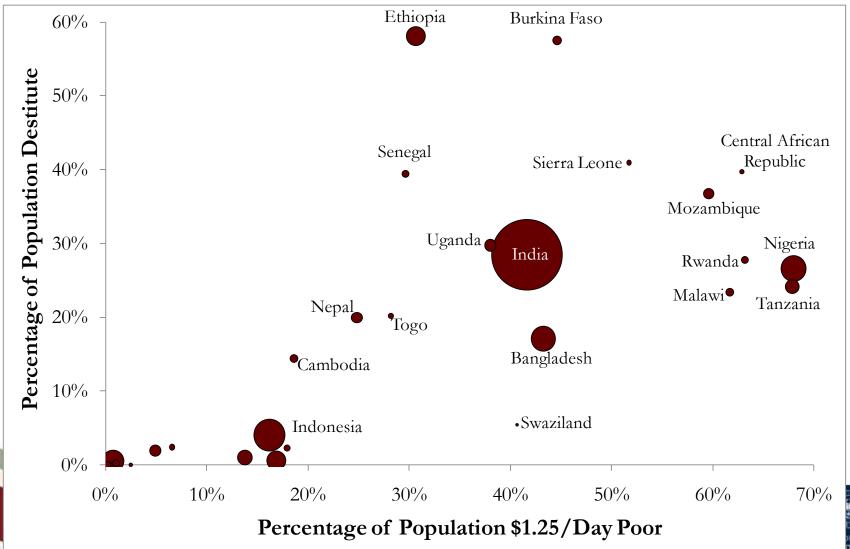
# Deprivations among the Destitute

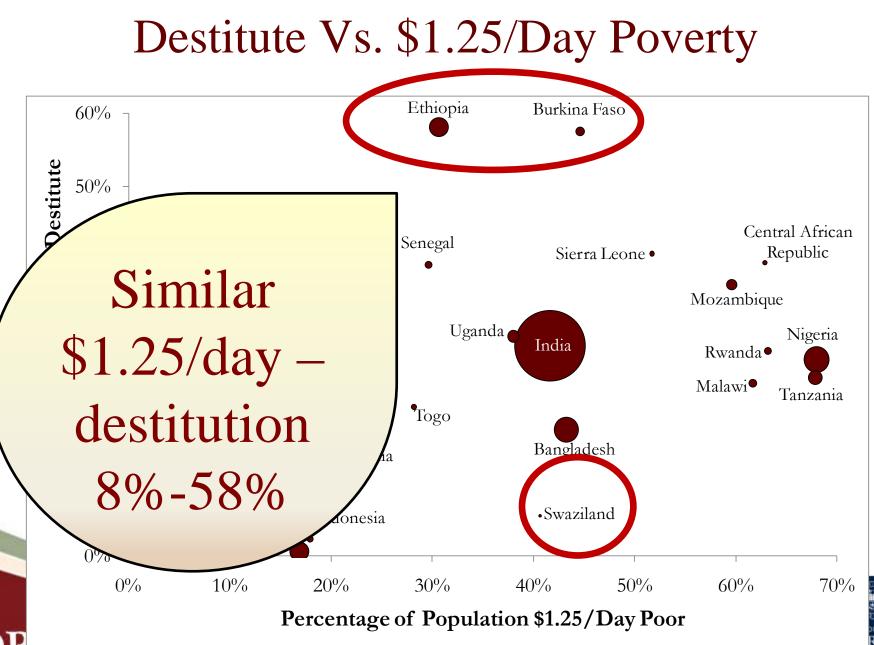
- 46% don't have anyone in their home with more than one year of schooling
- 36% have all primary-aged school children out of school
- 41% live in a household which has lost two or more children
- 67% have someone at home with severe malnutrition
- 71% don't have electricity to turn on the light
- 90% practice open defecation to relieve themselves

- 40% don't have clean water, or must walk 45 minutes to get it
- 83% have only a dirt floor
- 98% cook with wood, dung, or straw
- 69% don't even own a mobile phone or a radio nor a refrigerator or bike or television

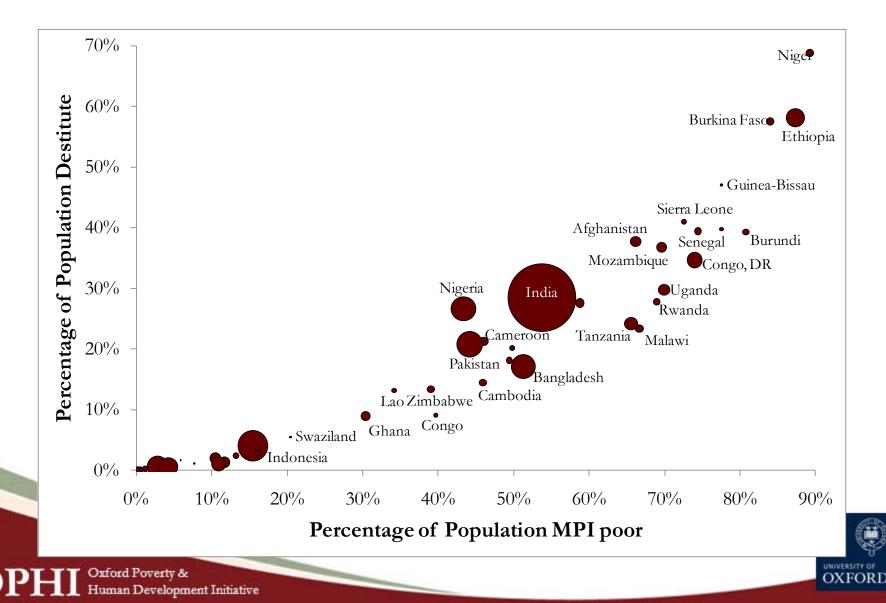


# Destitute Vs. \$1.25/Day Poverty

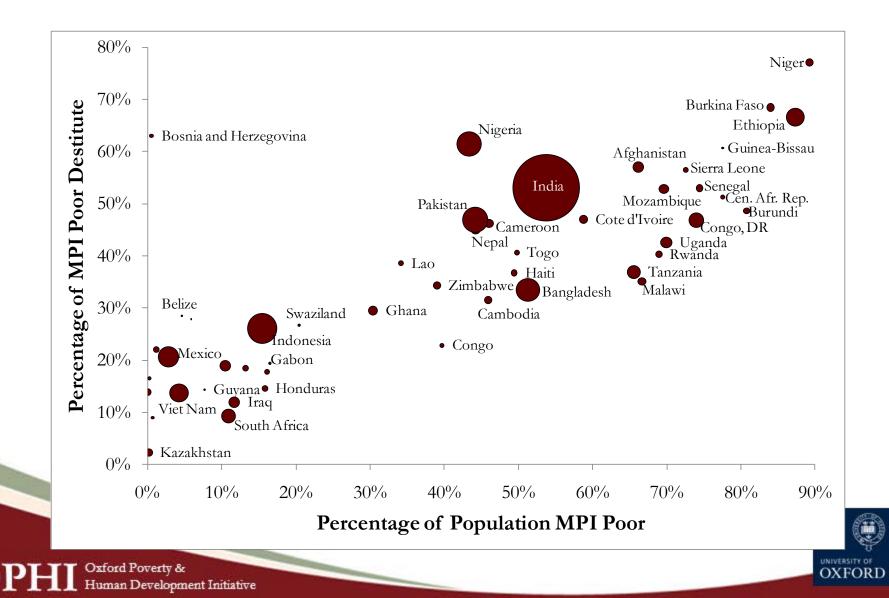




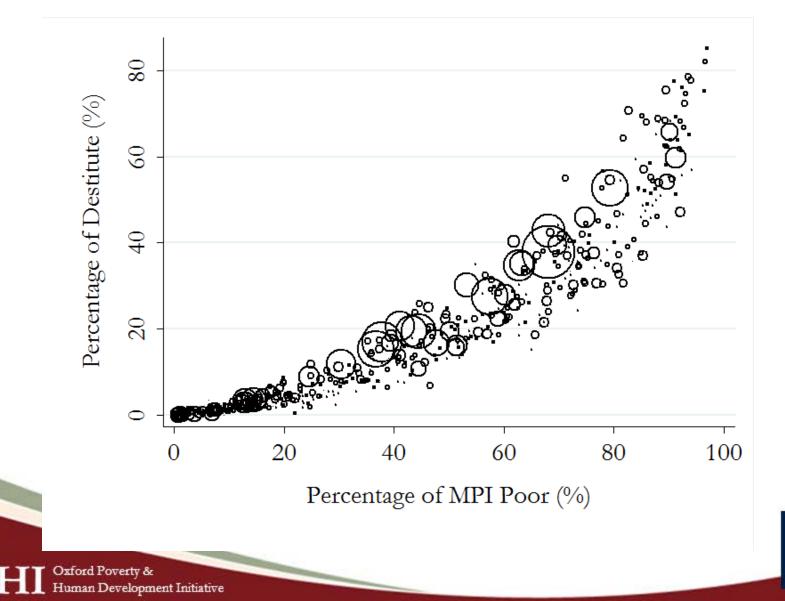
### MPI Poor vs. Destitute



# Destitute as Proportion of MPI Poor



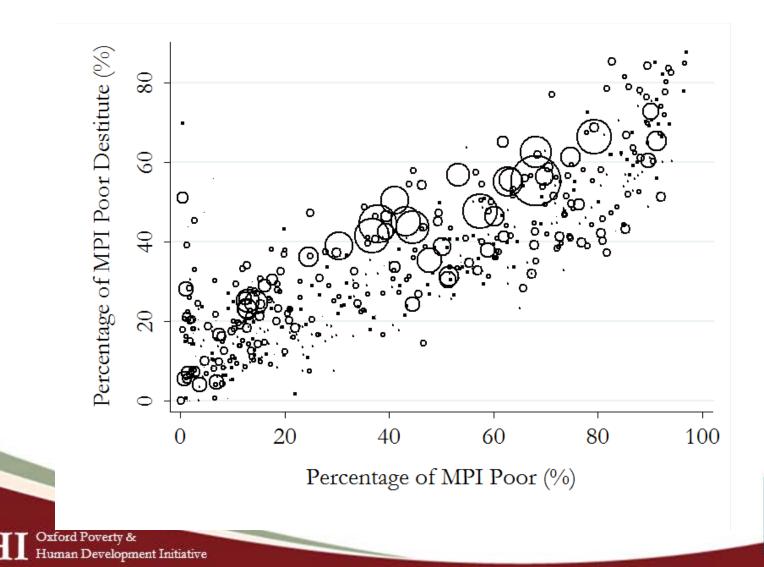
### MPI Poor vs. Destitute (Sub-national)



UNIVERSITY OF

OXFORE

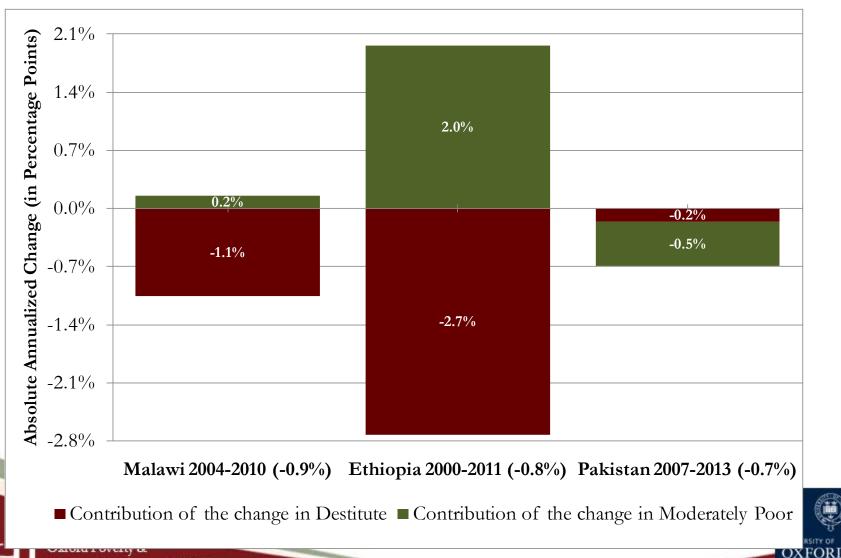
# Destitute as Proportion of MPI Poor (Sub-national)



UNIVERSITY O

OXFORI

# Breaking Down Changes in Overall Poverty



### Conclusions

We outline an approach in the counting approach framework to identify the destitute

Proper identification of the poorest of the poor is crucial in order to create adequate incentives to improve their conditions

Our application shows sobering large number of MPI poor are Destitute, facing extreme living conditions

