Conflicting Measures of Poverty and Inadequate Saving by the Poor
The Role of Status-Driven Utility Function
Sugata Marjit*
June 2012

Abstract
In the presence of inequality a status-driven utility function reconciles the conflict between income-based and nutrition-based measures of poverty. Moreover, it can explain why the poor tend to save less, an established empirical fact in the developing countries. The result is independent of the assumption of imperfect capital market. The paper attempts to integrate various strands of literature on status effects.

Keywords: inequality, inter-temporal consumer choice, utility, poverty

JEL Classification: D63, D91, D11, I3
Acknowledgements

The author is indebted to Pranab Kumar Das, Ravi Kanbur and Abhirup Sarkar, and seminar participants at ISI Delhi and Jadavpur University for comments. Thanks are also due to Dilip Mookherjee for making me aware of the relevant literature on status and bequests. The usual disclaimer applies.
1. **Introduction**

A fundamental query involving the preference pattern of any individual in a society has
to deal with the social influence on individual consumption behaviour. The idea of
conspicuous consumption and the so-called Veblen effect are quite well known in
economics. Very recently Sivanathan and Pettit (2010) have confirmed the fact that
individuals are quite sensitive to their relative status in the society and would like to
‘ mend’ their ‘self’, under constant attack from various social pressures, by taking
recourse to status-signaling consumption behaviour. A series of experiments confirm
such a pattern of human behaviour. This is one of the building blocks of the utility
function that we use and the subsequent analysis.

The paper starts off by highlighting a well-observed empirical phenomenon discussed
extensively in the literature on poverty in India. Patnaik (2007) and Deaton and Drèze
(2009) have dealt with the conflict between income-based measure and nutrition-based
measure of poverty. In India people moving above the poverty line with greater monthly
expenditure on overall consumption demonstrate lower nutritional intake. Thus Patnaik
(2007) asserts that actual poverty estimate is far greater than the optimistic figure
provided by the government. While Deaton and Drèze (2009) analyze various reasons
for such a behaviour, not much emphasis is given to the role of status-driven
consumption pattern, although they do not altogether ignore such a possibility. That
social inequality can influence individual’s consumption and induce greater
consumption of the so-called status good, becomes quite relevant for such analysis.
Thematically this is undermined and under-explored in the poverty literature. We shall
eventually demonstrate how preexisting social inequality can lead to the conflicting
measures of poverty.

Banerjee and Duflo (2007) reporting on various country studies have emphasized the
fact that in general the poor do not save what they should. In other words the bias
towards current consumption is a remarkably consistent empirical fact valid for a large
cross-section of the developing countries. Fafchamps ans Shilpi (2008) have
demonstrated how the presence of richer persons in a community affects the perceptions
of well being of the individuals. Such perception coupled with the status-driven
consumption behaviour can lead to a bias towards current consumption. The dynamic
extension of the basic framework yields this result without being dependent on further
complex assumptions.

In an interesting paper Moav and Neeman (2010) derive the inadequate saving result in
terms of a framework with bequests, as initially modeled in Galor and Zeira (1993).
They also use the notion of social status as a basic driving factor which via conspicuous
consumption affects current bequests and hence may perpetuate poverty trap. Essential
ingredient of this type of analysis is the existence of an imperfect credit market which
does not allow everyone to borrow and lend at a given rate of interest. In our framework
we abstract from all such complexities and use the evolution of social distribution of
income as a driving force.

One must mention that there is a literature on status and growth pioneered by Cole et al.
(1992) and later extended by Corneo and Jeanne (1998). The message of this literature
is that the aspiration effect i.e. the effort to attain higher status induces agent to over-
accumulate relative to the standard case i.e. without such concern for status. In a general
context, therefore, two offsetting effects must be considered, one that pushes the individual to consume more and the other when saving intensity is higher. We shall reflect on this issue in course of our analysis. Interestingly to highlight our concern we have a way to block the ‘over-accumulation effect’ due to concern for status.

A voluminous literature discusses the impact of social status, relative income and relative rewards on productivity such as Hopkins and Kornienko (2010), Ku and Salmon (2010), on optimal taxation such as Beath and Fitzroy (2010), Kabur and Tuomala (2010) and on network such as Ghiglino and Goyal (2008). However, these papers do not deal with the issues we are discussing in this paper.

The paper proceeds as follows. In the next section we discuss the issue of possible conflict between income and nutrition-based measures of poverty. In the third section we analyze the saving problem in a simple two-period framework. The last section concludes the paper.

2. Basic framework

We start from two possible axioms on how perceived social inequality affects the individual welfare.

Axiom 1: Inequality hurts

This implies that having below average income in a society reduces individual utility. Our assumption will be that being above average does not matter, but being below definitely hurts. This asymmetry is deliberate to highlight the implications of belonging to the downside of inequality.

Axiom 2: Inequality increases MU for status good

Having lower than average income increases the marginal utility of conspicuous consumption or consumption of the status good. This is directly drawn from experimental psychology literature where intensity of desire to consume the status good seems to be greater among those who are affected by social inequality.

We now invoke a simple log linear utility function with $N$, the consumption of nutrition good and $L$, the consumption of luxury or status good or non-nutrition good.

$$U = f \left( \frac{\bar{y}}{y} \right) \left[ \log N + \phi \left( \frac{\bar{y}}{y} \right) \log L \right]$$

(1)

$\bar{y}$ is average income of the reference social group. $y$ is individual income levels.

$$f \left( \frac{\bar{y}}{y} \right) \begin{cases} 1 & \text{for } y \geq \bar{y} \\ < 1 & \text{for } y < \bar{y} \end{cases}$$

(2)

and $f' < 0$. [Follows from Axiom 1]
\[ \phi \left( \frac{\bar{y}}{y} \right) = \begin{cases} 1 \text{ for } y \geq \bar{y} \\ > 1 \text{ for } y < \bar{y} \end{cases} \]  \hspace{1cm} (3) \\

and \( \phi' > 0 \). [Follows from Axiom 2] 

We shall not discuss price effect and assume prices to be equal to one.

If inequality truly hurts,

\[ f \left( \frac{\bar{y}}{y} \right) \left[ \log \bar{N} + \phi \left( \frac{\bar{y}}{y} \right) \log \bar{L} \right] < \left[ \log N_0 + \phi \left( \frac{\bar{y}}{y} \right) \log L_0 \right] \]  \hspace{1cm} (4) \\

Where \((\bar{N}, \bar{L})\) are optimal consumption levels for \( y < \bar{y} \) and \((N_0, L_0)\) are the same for the benchmark case with \( y = \bar{y} \).

Invoking the Envelope property it is straightforward to interpret \((U)\) as

\[ \frac{\partial u}{\partial y} = f' \left( -\frac{\bar{y}}{y^2} \right) \left( \log \bar{N} + \phi \left( \frac{\bar{y}}{y} \right) \log \bar{L} \right) + f \cdot \phi' \left( -\frac{\bar{y}}{y^2} \right) \log \bar{L} > 0 \]
Or, \[-\left(\frac{y}{y^2}\right)f' \log(N) - \left(\frac{y}{y^2}\right) \log \tilde{L} [f' \phi + f \phi'] > 0\]

Since \(f' < 0\) and \(\phi' > 0\), a sufficient condition is given by

\[
[f' \phi + f \phi'] < 0
\]  \hspace{1cm} (5)

Note that if \(y\) moves up the ladder \(f(.)\) increases but \(\phi\) drops. Or put differently if \(y\) drops from \(\tilde{y}\), \(f\) goes down to a value less than 1, but \(\phi\) increases, the net effect has to be negative if inequality has to hurt in equilibrium. We shall return to condition (5) later.

It is obvious that in equilibrium

\[
\tilde{N} = \frac{y}{1 + \phi}
\]  \hspace{1cm} (6)

\(y\) is assumed to be large enough to make the log value in (6) positive.

We are interested in the level of consumption of \(N\) as \(y\) increases from below \(\tilde{y}\). Given \(\left(\frac{\tilde{y}}{y}\right)\), (6) is a very standard outcome. When \(\phi = 1\), by virtue of having this specific utility function, \(\tilde{N} = \frac{1}{2} y\). However, when \(\phi > 1\) and if both \(y\) and \(\tilde{y}\) increase when we increase \(y\), relative social status can worsen leading to an increase in \(\phi\) and a net reduction in \(\tilde{N}\).

\[
\frac{d^2 N}{dy^2} < 0 \text{ iff } \mu \sigma > \frac{1 + \phi}{\phi}
\]  \hspace{1cm} (7)

Where, \(\mu = \frac{d\phi}{d\left(\frac{\tilde{y}}{y}\right)} \frac{\tilde{y}/y}{\phi} \) and \(\sigma = \frac{d\left(\frac{\tilde{y}}{y}\right)}{dy} \frac{y}{\tilde{y}/y} \).

As \(y \rightarrow \tilde{y}, \phi \left(\frac{\tilde{y}}{y}\right) \rightarrow 1, \frac{1 + \phi}{\phi} \rightarrow 2\).

As \(y \rightarrow 0, \phi \left(\frac{\tilde{y}}{y}\right) \rightarrow \infty, \frac{1 + \phi}{\phi} \rightarrow 1\).
If \( \left( \frac{y}{y} \right) \) increases with \( y \), the consumption of \( N \) reacts according to the magnitude of \( \mu \) and \( \sigma \). While \( \mu \) reflects the cultural perception of relative status, \( \sigma \) reflects the elasticity of distribution. If either of them is very weak, we should not have any conflict of measures of poverty. If either of them is zero, we are back with the standard case. If either of them is very high we shall have our interesting results. Also greater is \( \left( \frac{y}{y} \right) \) and lower is \( \frac{1}{\phi} \) chances are greater that the conflict will arise. Inequality has a direct bearing on the nutritional estimate of poverty.

3. **Dynamic behaviour**

We shall now highlight the case of inadequate saving by the poor. In fact in our framework we do not need any assumption regarding the behaviour of the capital market. We use a simple two-period model which can have a ‘present and future’ interpretation. We have a small open economy where product prices are frozen from the rest of the world. Agents can borrow and lend at an exogenously specified rate of return. Agents can also accumulate capital. The simple two-period model brings out certain essential dynamic features regarding rate of accumulation, status effect and saving.

Two time periods are denoted by subscripts 1 and 2.
The problem facing the agent

$$\max_{\{N_1,L_1,N_2,L_2,K\}} f \left( \frac{\bar{y}_1}{y_1} \right) \left[ \log N_1 + \phi \left( \frac{\bar{y}_1}{y_1} \right) \log L_1 \right] + \beta f \left( \frac{\bar{y}_2}{y_2} \right) \left[ \log N_2 + \phi_2 \log L_2 \right]$$

Subject to,

$$(y_1 - N_1 - L_1, -K) (1 + r) + y_2(K) - N_2 - L_2 = 0$$

Where, $\bar{y}_2 = y_2(K) + s(1 + r)$ and $s = (y_1 - N_1 - L_1, -K)$. K stands for investment. $y_1$ is considered as given to start with and $0 < \beta < 1$ is the discount factor.

Optimization and simple manipulations yield

$$\frac{\bar{f}_1}{N_1} + \beta A (1 + r) = \beta \frac{\bar{f}_2}{N_2} (1 + r) \tag{8}$$

Where $A = [\beta \phi_2 \left( \frac{\bar{y}_1}{y_2} \right) (1 + r) \Omega_2 + \beta \phi_2 \phi_2 \left( \frac{\bar{y}_1}{y_2} \right) (1 + r) \log \bar{L}_2]$.

$\Omega_2 =$ optimal value of the second period utility.

$\{\bar{N}_1, \bar{L}_1, \bar{N}_2, \bar{L}_2, \bar{K}\}$ are to be treated as optimal values.

From (5) it follows that $A < 0$.

Now,

$$\bar{N}_2 = \frac{N_1(1+r)\beta \phi_2}{f_1 + \beta A N_1(1+r)} \tag{9}$$

Similarly,

$$\bar{L}_2 = \frac{L_1(1+r)\beta \phi_2}{f_1 \phi_1 + \beta A L_1(1+r)} \tag{10}$$

Also note that, $y_2'(\bar{K}) = (1 + r) \tag{11}$

Equation (11) is a significant condition because even if increasing $\bar{K}$ improves future utility apart from income, so long as $r$ is given exogenously, the rate of accumulation does not change. Note the difference between this structure and the status-driven growth models. Social status is likely to increase $K$, but given that the alternative return is $(1+r)$ as derived from the bond, marginal product must adjust to $(1+r)$. thus the level of $K$ remains the same with or without concerns for status as long as $r$ does not change.
Let us now compare the amount of savings with or without concerns for social status.

\[ \tilde{N}_1 + \tilde{L}_1 + \frac{\hat{S}_1(1+r)\beta f_2}{f_1 + \beta A \tilde{N}_1(1+r)} + \frac{L_1(1+r)\beta f_2 \phi_2}{f_1 \phi_1 + \beta A \tilde{L}_1(1+r)} = y_1 - \tilde{K} + \frac{y_2(K)}{(1+r)} \equiv R(\tilde{K}) \]  

(12)

With \( f = \phi_1 = 1 \) and \( A=0 \) we get the standard outcome.

\[ N_1^0 + L_1^0 = \frac{R(K^0)}{(1+\beta)} \]  

(13)

Note that, \( K^0 = \tilde{K} \)

Therefore,

\[ \tilde{N}_1 + \tilde{L}_1 + \frac{1}{(1+\beta)} \left[ \frac{\tilde{N}_1 \beta f_2}{f_1 + \beta A \tilde{N}_1(1+r)} - \beta \tilde{N}_1 \right] + \frac{1}{(1+\beta)} \left[ \frac{\tilde{L}_1 \beta f_2 \phi_2}{f_1 \phi_1 + \beta A \tilde{L}_1(1+r)} - \beta \tilde{L}_1 \right] = N_1^0 + L_1^0 \]  

(14)

Two sources of saving \( S \) and \( K \) are financed by \( [y_1 - (\tilde{N}_1 + \tilde{L}_1)] \), therefore a direct comparison between \((\tilde{N}_1 + \tilde{L}_1)\) and \((N_1^0 + L_1^0)\) will be relevant.

(14) suggests the following

A set of sufficient conditions, that guarantee aggregate saving to be lower in the case with the concern for social status, are

\[ f_2 < f_1 + \beta A \tilde{N}_1(1+r) \] \[ f_2 \phi_2 < f_1 \phi_1 + \beta A \tilde{L}_1(1+r) \]  

(15)

Consider the case that the income distribution is invariant over time i.e. \( f_1 = f_2 \) and \( \phi_1 = \phi_2 \). They can still be less than 1 as \( \bar{y} > y \). [If \( f_1 = f_2 = \phi_1 = \phi_2 = 1 \), then we are dealing with the standard case.] under this situation (15) can never hold as \( A<0 \). Therefore saving will be greater than in the normal case. Strong implication of this observation is that if social inequality is not changing overtime, agents wish to save more to improve their situation. Even if extra dose of \( K \) is not forthcoming as \( K^0 = \tilde{K} \), saving in terms of the other asset should be greater. This is also the basic intuition behind status-driven growth literature, the so-called positive effect of concern for status. Better status gives better utility.

Next consider the case that ceteris paribus, \( \bar{y}_2 \) is really high relative to \( \bar{y}_1 \) i.e. the rest of the society, possibly those with income level much greater than the agent are going to grow substantially so that \( f_2 \) is really low relative to \( f_1 \) and \( f_2 \phi_2 \) relative to \( f_1 \phi_1 \), then (15) will hold and \( (\tilde{N}_1 + \tilde{L}_1) > (N_1^0 + L_1^0) \). Therefore, aggregate saving will be lower. The intuition is that if the agents perceive that their social status will be eroded substantially in the future they will prepare their consumption reducing saving.
Consider the case where $f$ and $\phi$ matter but not their change. So $f_2' = \phi_2' \equiv 0$. this will make $A \equiv 0$. Then it is entirely between $f_1$ and $f_2$ or $f_1 \phi_1$ and $f_2 \phi_2$ and how low is $f_2$ relative to $f_1$. Thus apprehension about future has a direct impact on current saving.

If we wish to compare the static and dynamic case one feature is very clear. In the poverty problem $\phi$ is very important in determining the trade-off between $N$ and $L$ whereas in the dynamic case it is really $f$ that is critical.

4. Concluding remarks

The purpose of this paper has been twofold. First, to provide a theoretical explanation behind the conflict between nutrition and income-based measures of when consumption depends on relative income status. The second motivation has to do with the relevance of status-driven consumption behaviour leading to inadequacy of saving by the poor. The simple dynamic model identifies the trade-off between saving augmenting and saving reducing effects of social status.

The log-linear utility function we work with yields standard outcomes when the concern for social status is absent. But drastic alteration of results is possible when we introduce the idea of relative social status in an otherwise simple utility function.

The large body of literature has discussed various types of economic problems under the assumption of concern for relative social status. Our approach is specific and focused. The result on the measurement of poverty yields a theoretical insight towards one of the most worrying consequence of growth. The result on saving is derived independent of any added assumption on credit market or any other behavioural assumption such as bequests.
References


